

Section 6.4 Answers

$$1) \log_3(9) = 2$$

$$3) \log_3(81) = 4$$

$$5) \log_3 \frac{1}{3} = -1$$

$$7) \ln(x) = y$$

$$9) \ln(20.09) = 3$$

$$11) \ln(2.72) = 1$$

$$13) 3^4 = 81$$

$$15) 2^6 = 64$$

$$17) 6^1 = 6$$

$$19) 10^3 = x$$

$$21) e^1 = x$$

$$23) e^w = 2x$$

$$25) e^2 = e^2$$

$$27) 1$$

$$29) 1$$

$$31) 0$$

$$33) 0$$

$$35) 3$$

$$37) 1$$

$$39) 0$$

$$41) 2$$

$$43) 7$$

$$45) 3$$

$$47) 6$$

$$49) 5$$

$$51) 1$$

$$53) 3$$

$$55) -2$$

$$57) .7782$$

$$59) -.4771$$

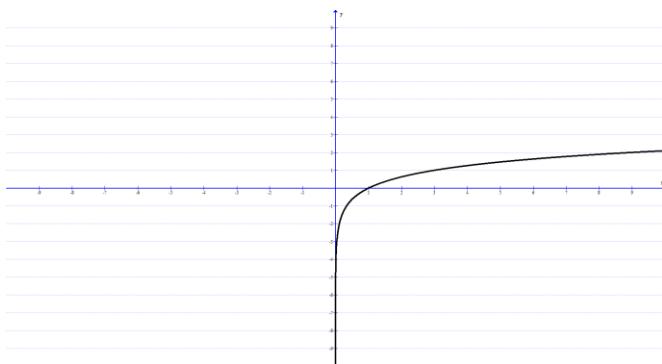
$$61) -2.0969$$

$$63) 1.9459$$

$$65) 2.7726$$

67a)

x	y	point
3^2	2	(9,2)
3^1	1	(3,1)
3^0	0	(1,0)
3^{-1}	-1	(1/3, -1)
3^{-2}	-2	(1/9, -2)



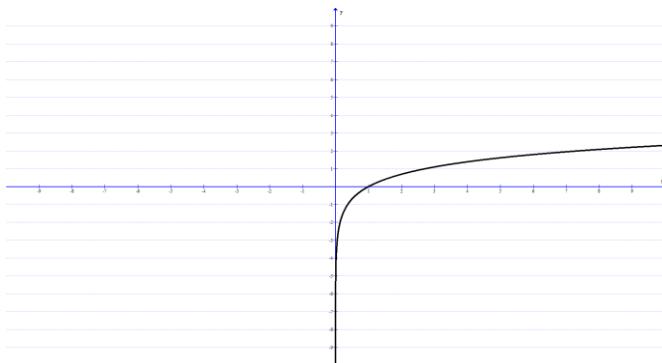
b) State the domain of each function.

67b) domain: $(0, \infty)$

69a)

Create a table of values, I will put the numbers 2,1,0,-1,-2 in the y column and solve for x.

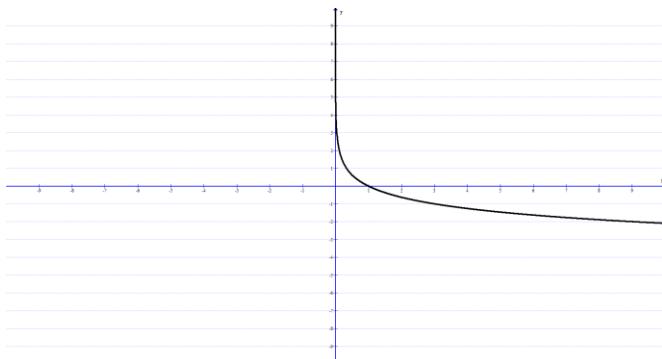
x	y	point
e^2	2	(7.39, 2)
e^1	1	(2.72, 1)
e^0	0	(1, 0)
e^{-1}	-1	(.37, -1)
e^{-2}	-2	(.14, -2)



69b) domain $(0, \infty)$

71a)

x	y	point
$\left(\frac{1}{3}\right)^2$	2	(1/9, 2)
$\left(\frac{1}{3}\right)^1$	1	(1/3, 1)
$\left(\frac{1}{3}\right)^0$	0	(1, 0)
$\left(\frac{1}{3}\right)^{-1}$	-1	(3, -1)
$\left(\frac{1}{3}\right)^{-2}$	-2	(9, -2)



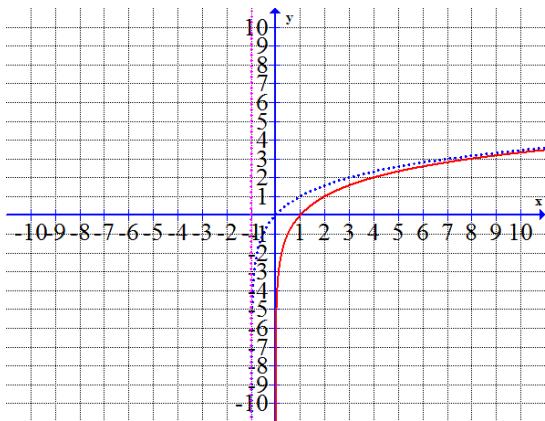
71b) domain $(0, \infty)$

73a) $f(x + 1) = \log_2(x + 1)$

73b) $x > -1$ or $(-1, \infty)$

73c) shifts left 1

73d) Graph of $f(x + 1)$ drawn in blue

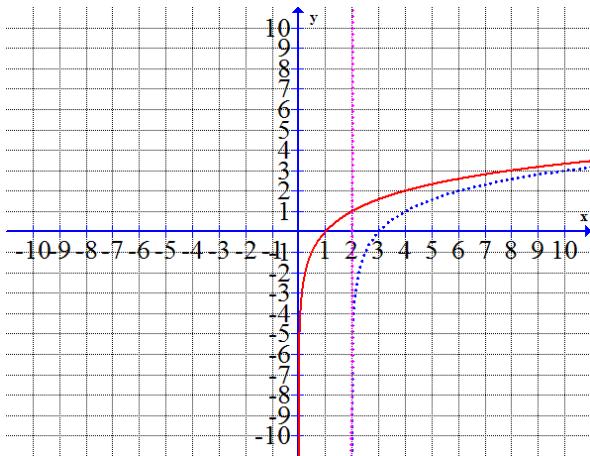


75a) $f(x - 2) = \log_2(x - 2)$

75b) $x > 2$ or $(2, \infty)$

75c) Shifts right 2

75d)



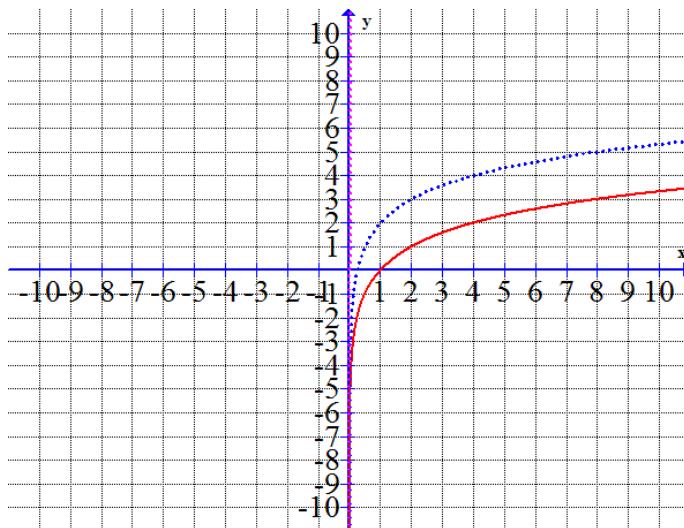
77a) $f(x) + 2 = \log_2(x) + 2$

77b) $x > 0$ or $(0, \infty)$

77c) shifted up 2 units

77d) Just shift each point in the graph of $f(x)$ two units to the up. I showed the $x > 0$ domain as a vertical asymptote drawn in purple. The graph will not exist to the left of this vertical line $x = 0$.

Graph of $f(x) + 2$ drawn in blue



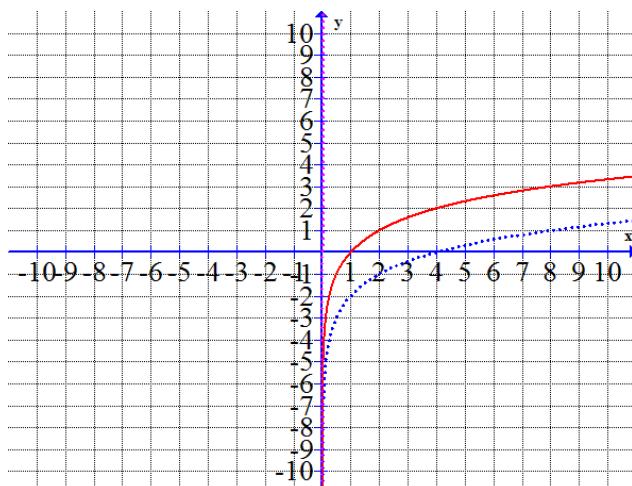
79a) $f(x) - 2 = \log_2(x) - 2$

79b) $x > 0$ or $(0, \infty)$

79c) Shifted down 2 units

79d) Just shift each point in the graph of $f(x)$ two units to the down. I showed the $x > 0$ domain as a vertical asymptote drawn in purple. The graph will not exist to the left of this vertical line $x = 0$.

Graph of $f(x) - 2$ drawn in blue



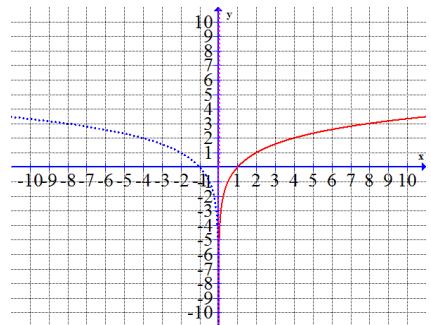
81a) $f(-x) = \log_2(-x)$

81b) any of these three answers are correct, you only need to give one answer.

$0 > x$ or $x < 0$ or $(-\infty, 0)$

81c) reflects over the y-axis

81d) Just reflect each point over the y-axis. The graph will now only exist to the left of the y-axis. The vertical asymptote will still be at $x = 0$ (or the y-axis). It's now the right edge of the graph as opposed to the left edge of the graph.



83a) $3f(x) = 3\log_2(x)$

83b) $x > 0$ or $(0, \infty)$

83c) stretches the graph

83d) This is a non-rigid transformation. I need to make a table of values to sketch an accurate graph.

We can use the x's from the given table. We create y's by multiplying each y-value by 3.

<p>3f(x) is drawn in blue. The vertical asymptote is drawn in purple.</p>	<p>Here are the points that are marked in the original graph</p> <table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="text-align: left; padding: 5px;">x</th><th style="text-align: left; padding: 5px;">$f(x)$</th></tr> </thead> <tbody> <tr> <td style="padding: 5px;">.25</td><td style="padding: 5px;">-2</td></tr> <tr> <td style="padding: 5px;">.5</td><td style="padding: 5px;">-1</td></tr> <tr> <td style="padding: 5px;">1</td><td style="padding: 5px;">0</td></tr> <tr> <td style="padding: 5px;">2</td><td style="padding: 5px;">1</td></tr> <tr> <td style="padding: 5px;">4</td><td style="padding: 5px;">2</td></tr> </tbody> </table> <p>The table for $3f(x)$ will have the same x-values, but the y's will be multiplied by 3.</p> <p>Here is the table for $3f(x)$</p> <table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="text-align: left; padding: 5px;">x</th><th style="text-align: left; padding: 5px;">$3f(x)$</th></tr> </thead> <tbody> <tr> <td style="padding: 5px;">.25</td><td style="padding: 5px;">-6</td></tr> <tr> <td style="padding: 5px;">.5</td><td style="padding: 5px;">-3</td></tr> <tr> <td style="padding: 5px;">1</td><td style="padding: 5px;">0</td></tr> <tr> <td style="padding: 5px;">2</td><td style="padding: 5px;">3</td></tr> <tr> <td style="padding: 5px;">4</td><td style="padding: 5px;">6</td></tr> </tbody> </table>	x	$f(x)$.25	-2	.5	-1	1	0	2	1	4	2	x	$3f(x)$.25	-6	.5	-3	1	0	2	3	4	6
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